

REPORT DOCUMENTATION PAGE		READ INSTRUCTIONS BEFORE COMPLETING FORM
1. REPORT NUMBER ALGO_PUB_0097	2. GOVT ACCESSION NO.	3. RECIPIENT'S CATALOG NUMBER
4. TITLE (and Subtitle) Technical Memo 27, 'Extension of Computer Based Algorithms by Operator Analysts'		5. TYPE OF REPORT & PERIOD COVERED FINAL
7. AUTHOR(s) Mathematical Analysis Research Corp. (MARC)		6. PERFORMING ORG. REPORT NUMBER D-4624
9. PERFORMING ORGANIZATION NAME AND ADDRESS Jet Propulsion Laboratory, ATTN: 171-209 California Institute of Technology 4800 Oak Grove, Pasadena, CA 91109		8. CONTRACT OR GRANT NUMBER(s) NAS7-918
11. CONTROLLING OFFICE NAME AND ADDRESS Commander, USAICS ATTN: ATSI-CD-SF Ft. Huachuca, AZ 85613-7000		10. PROGRAM ELEMENT, PROJECT, TASK AREA & WORK UNIT NUMBERS RE 182 AMEND #187
14. MONITORING AGENCY NAME & ADDRESS (if different from Controlling Office) Commander, USAICS ATTN: ATSI-CD-SF Ft. Huachuca, AZ 85613-7000		12. REPORT DATE 28 Apr 87
		13. NUMBER OF PAGES 7
16. DISTRIBUTION STATEMENT (of this Report)  Approved for Public Dissemination		15. SECURITY CLASS. (of this report) UNCLASSIFIED
		15a. DECLASSIFICATION/DOWNGRADING SCHEDULE NONE
17. DISTRIBUTION STATEMENT (of the abstract entered in Block 20, if different from Report)		
18. SUPPLEMENTARY NOTES  Prepared by Jet Propulsion Laboratory for the US Army Intelligence Center and School's Combat Developer's Support Facility.		
19. KEY WORDS (Continue on reverse side if necessary and identify by block number)  Fix Estimation Algorithms, Operator Training, Bias, Variance		
20. ABSTRACT (Continue on reverse side if necessary and identify by block number)  This report discusses limitations of algorithms with respect to operator training. Operators can improve algorithm performance thru use of unmodeled data (weather, history of variance, etc.). As an example fixing bias is discussed in detail.		

7057-72

U.S. ARMY INTELLIGENCE CENTER AND SCHOOL  
Software Analysis and Management System

Extension Of Computer Based Algorithms  
By Operator Analysts

Technical Memorandum No. 27

28 April 1987

Author:

Murray W. Rennel  
MARC  
Mathematical Analysis Research Corporation

Approval:

JWG  
James W. Gillis, Subgroup Leader  
Algorithm Analysis Subgroup

Edward Records  
Edward J. Records, Supervisor  
USAMS Task

Concur:

A. F. Ellman  
A. F. Ellman, Manager  
Ground Data Systems Section

F. V. Vote  
Fred Vote, Manager  
Advanced Tactical Systems

JET PROPULSION LABORATORY  
California Institute of Technology  
Pasadena, California

JPL D-4624

## PREFACE

The work described in this publication was performed by the Mathematical Analysis Research Corporation (MARC) under contract to the Jet Propulsion Laboratory, an operating division of the California Institute of Technology. This activity is sponsored by the Jet Propulsion Laboratory under contract NAS7-918, RE182, A187 with the National Aeronautics and Space Administration, for the United States Army Intelligence Center and School.

This specific work was performed in accordance with the FY-87 statement of work (SOW #2).

Accession For	
NTIS GRA&I	<input checked="" type="checkbox"/>
DTIC TAB	<input type="checkbox"/>
Unannounced	<input type="checkbox"/>
Justification	
By	
Distribution/	
Availability Codes	
Dist	Avail and/or Special
A-1	



## **EXECUTIVE SUMMARY**

This Technical Memorandum was prepared to summarize the results of work performed under both the FY-86 and FY-87 Statements of Work and was funded by the FY-86 funds.

The purpose of this Technical Memorandum is to clarify the desirable interactions between computer-based algorithms and their operators necessary to optimize their combined effectiveness.

## Extension Of Computer Based Algorithms By Operator Analysts

### SUMMARY

Algorithm development should have two phases: The computer portion and the portion to be incorporated in operator analyst training.

A knowledgeable operator analyst should be able to perform analysis beyond the means of any particular computerized algorithm available to that analyst. This follows from the fact that humans can understand the consequences of the limitations of particular computer implementations and correct, in part, for them.

Computer based algorithm limitations may have different causes:

- 1)  $\leftrightarrow$  The algorithms may be based on incomplete or inaccurate models;
- 2)  $\leftrightarrow$  The algorithms may not be flexible enough to adapt to the need for changes in analysis criteria;
- 3)  $\leftrightarrow$  The algorithms may take shortcuts because of limitations in computer storage or speed;
- 4)  $\leftrightarrow$  There may be refinements in the analysis which could be computed but are not because they depend on parameters which are insufficiently well known; and
- 5)  $\leftrightarrow$  Computer output formats may be restrictive. *Keywords:*

It is out of the scope of this memo to illustrate the multitude of variations on the limitations discussed above. Instead one example will be discussed at some length in the sections that follow.

### INTRODUCTION TO THE EXAMPLE- BIAS IN FIX ALGORITHMS

#### Intuitive Definition of Bias-

For simplicity assume there is no difficulty deciding which bearings to use in a fix. If there were no angular error in bearing measurements, then the fix location would be the true location in any reasonable algorithm. A given fix may be near or far from the true emitter location depending on the particular set of angular errors that one actually observes. This set of angular errors is only one of many possible combinations, each yielding a different fix. One hopes that the average<sup>1</sup> of the fixes that might have occurred is near the true location of the emitter. Sometimes it isn't. Whether it is or isn't the difference between the average expected location and the true location is called the bias of the fix.

<sup>1</sup> Weighted by their likelihood of occurrence.

*in estimation, i.e.,  
Variance. (kg)*

### Minimizing Bias

Zero bias is not a realistic objective. Small bias may be possible, however. Bias may be considered small if either

- 1) it is much smaller than typical random error
- 2) it is much smaller than application requirements  
(targeting, fusion or whatever)

Bias size can be made smaller by either

- 1) using a better fix algorithm
- 2) using more accurate bearings
- 3) using bearings at a wider range of angles relative to the emitter (often accomplished using a longer base-line) and not permitting the bearings from the middle angles to dominate the fix

In practice there are limits to the extent that these three approaches can be applied. In the case of algorithms for example, the limiting factors are of two types:

- 1) Speed and storage requirements for an algorithm exceeding hardware capabilities.
- 2) A parameter (angular standard deviation) used in models which is not really known but also not sufficiently unknown to be treated as coming solely from the data. Corrections for bias would be possible if this parameter were known.

### ANALYST CONTRIBUTIONS

Even though knowledge of factors causing bias is not exact enough for calculating corrections, the analyst can get a rough feel for it based on:

- 1) The analyst can know the factors affecting the accuracy not incorporated in the model (such as weather).
- 2) The analyst can know more about the angular standard deviation parameter than is used in the calculation. He knows, for example, the history of accuracy.
- 3) The analyst can know patterns in the behavior of the fix algorithm, for example,
  - a) The most commonly used algorithms are biased short.
  - b) Fixes with narrower ellipses have larger bias.
- 4) The analyst may be able to imagine a range of possible biases and qualify decision making on it without actually knowing how large bias actually is.